## Computer Science 456/656: the Pumping Lemmas

**Pumping Lemma for Regular Languages.** For any regular language LThere exists a number p (called the *pumping length* of L such that For any string  $w \in L$  of length at least pThere exist strings x, y, and z such that

- 1. xyz = w
- 2.  $|xy| \leq p$
- 3. y is not the empty string
- 4. For any integer  $i \ge 0$   $xy^i z \in L$

**Pumping Lemma for Context-Free Languages.** For any context-free language LThere exists a number p (called the *pumping length* of L such that For any string  $w \in L$  of length at least pThere exist strings u, v, x, y, and z such that

- 1. uvxyz = w
- 2.  $|vxy| \leq p$
- 3. v and y are not both the empty string
- 4. For any integer  $i \ge 0$   $uv^i xy^i z \in L$