Homework 
$$\#2$$
  
Due Th.  $9/18$ 

- 1. Find the z-transform for each of the following sequences and indicate which also have a DTFT.
  - (a)  $x[n] = 3\delta[n] + \delta[n-2] + \delta[n+2]$
  - (b) x[n] = u[n] u[n 10]
  - (c)  $x[n] = (\frac{1}{3})^n u(-n)$
  - (d)  $x[n] = \left(\frac{1}{2}\right)^n u(n+2) + (3)^n u(-n-1)$
  - (e)  $x[n] = \alpha^{|n|}$
  - (f)  $x[n] = n \left(\frac{1}{2}\right)^n u[n-2]$
- 2. Find the z-transform of the sequence  $y[n] = \sum_{k=\infty}^{n} x[k]$  in terms of the z-transform of x[n].
- 3. Use the z-transform to perform the convolution of

$$h[n] = \begin{cases} \left(\frac{1}{2}\right)^n & 0 \le n \le 2\\ 0 & else \end{cases}$$
$$x[n] = \delta[n] + \delta[n-1] + 4\delta[n-2]$$

4. Evaluate the convolution of the following sequences

$$h[n] = (0.5)^n u[n]$$
  $x[n] = 3^n u[-n]$ 

- 5. Find the inverse of the following z-transforms and indicate which also have a DTFT
  - (a)  $X(z) = 4 + 3(z^2 + z^{-2})$   $0 < |z| < \infty$
  - (b)  $X(z) = \frac{1}{1 \frac{1}{2}z^{-1}} + \frac{3}{1 \frac{1}{3}z^{-1}}$   $|z| > \frac{1}{2}$
  - (c)  $X(z) = \frac{1}{1+3z^{-1}+2z^{-2}}$  |z| > 2
  - (d)  $X(z) = \frac{1}{(1-z^{-1})(1-z^{-2})} + |z| > 1$
- 6. A digital filter is described by the linear constant coefficient difference equation

$$y[n] = \frac{3}{4}y[n-1] - \frac{1}{8}y[n-2] + x[n].$$

The impulse response of the filter is measured with initial conditions

$$y[-1] = -1$$
  $y[-2] = 1.$ 

Determine the measured response of the filter and compare it with the zero state response.