EE795: Computer Vision and Intelligent Systems

Spring 2012

TTh 17:30-18:45 WRI C225

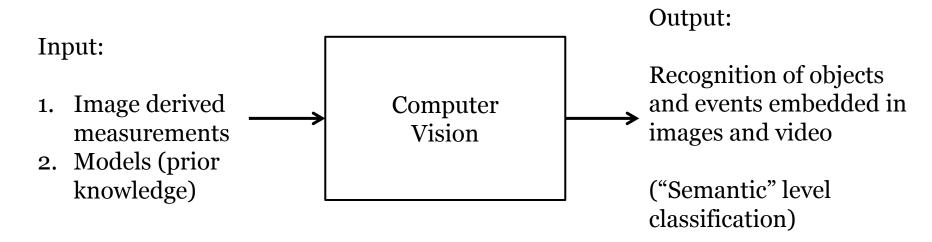
Lecture 03 130129

Outline

- Review
- Histogram Equalization
- Image Filtering
- Linear Filtering
- Morphology
- Connected Components

Computer Vision

Interpretation and understanding of images



Examples:

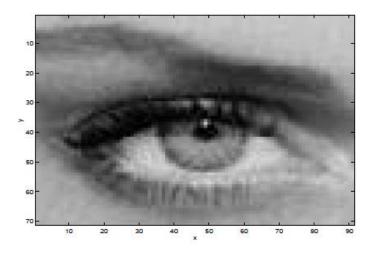
- Object recognition
- Face recognition
- Lane detection
- Activity analysis

Image as Function

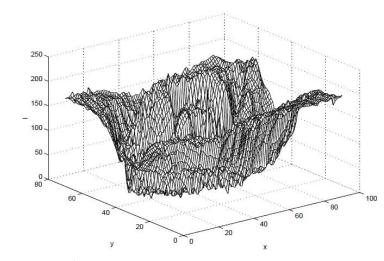
- Image is a function, f, that maps from R^2 to R
 - 0 < f(x, y) < 1 is the intensity at a point (x, y)
 - In reality, an image is defined over a rectangle with a finite range of values
 - $f:[a,b]\times[c,d]\rightarrow[0,1]$
- Computationally, [0,1] range is convenient but usually we have an 8-bit quantized representation
 - 0 < f(x, y) < 255
- Color image is just three separate functions pasted together
 - f(x,y) = [r(x,y); g(x,y); b(x,y)]

Image as Function

- Multiple equivalent representations
- Image



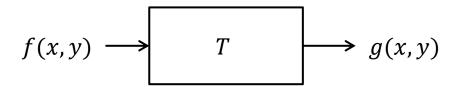
Surface



Matrix

Image Processing

- Usually the first stage of computer vision applications
 - Input an image to a system → get a processed image as output



$$g(x,y) = T[f(x,y)]$$

Digital Image Processing by Gonzalez and Woods is a great book to learn more

Pixel Transforms

- Gain and bias (Multiplication and addition of constant)
 - g(x,y) = a(x,y)f(x,y) + b(x,y)
 - a (gain) controls contrast
 - b (bias) controls brightness
 - Notice parameters can vary spatially (think gradients)
- Linear blend
 - $g(x) = (1 \alpha)f_0(x) + \alpha f_1(x)$
 - We will see this used later for motion detection in video processing

Compositing and Matting

- Techniques to remove an object and place it in a new scene
 - E.g. blue screen









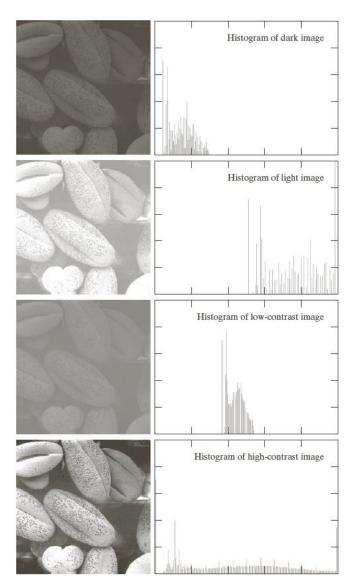
- Matting extracting an object from an original image
- Compositing inserting object into another image (without visible artifacts)
- A fourth alpha channel is added to an RGB image
 - α describes the opacity (opposite of transparency) of a pixel
- Over operator
 - $C = (1 \alpha)B + \alpha F$



Histogram Processing

- Digital image histogram is the count of pixels in an image having a particular value in range [0, L-1]
 - $h(r_k) = n_k$
 - r_k the kth gray level value
 - Set of r_k are known as the bins of the histogram
 - n_k the numbers of pixels with kth gray level
- Empirical probability of gray level occurrence is obtained by normalizing the histogram
 - $p(r_k) = n_k/n$
 - n total number of pixels

Histogram Example



- x-axis intensity value
 - Bins [0, 255]
- y-axis count of pixels
- Dark image
 - Concentration in lower values
- Bright image
 - Concentration in higher values
- Low-contrast image
 - Narrow band of values
- High-contrast image
 - Intensity values in wide band

Histogram Equalization

- Assume continuous functions (rather than discrete images)
- Define a transformation of the intensity values to "equalize" each pixel in the image
 - s = T(r) $0 \le r \le 1$
 - Notice: intensity values are normalized between 0 and 1
- The inverse transformation is given as
 - $r = T^{-1}(s) \quad 0 \le s \le 1$
- Viewing the gray level of an image as a random variable
 - $p_s(s) = p_r(r) \left| \frac{dr}{ds} \right|$

 Let s by the cumulative distribution function (CDF)

$$s = T(r) = \int_0^r p_r(w) dw$$

Then

$$\frac{ds}{dr} = p_r(r)$$

- Which results in a uniform
 PDF for the output intensity
 - $p_{s}(s) = 1$
- Hence, using the CDF of a histogram will "equalize" an image
 - Make the resulting histogram flat across all intensity levels

Discrete Histogram Equalization

 The probability density is approximated by the normalized histogram

$$p_r(r_k) = \frac{n_k}{n}$$
 $k = 0, ..., L-1$

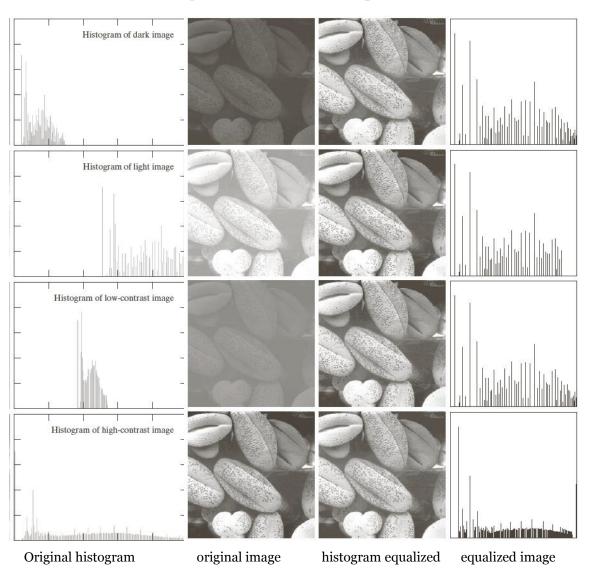
The discrete CDF transformation is

$$s_k = T(r_k) = \sum_{j=0}^k p_r(r_j)$$

$$S_k = \sum_{j=0}^k \frac{n_k}{n}$$

- This transformation does not guarantee a uniform histogram in the discrete case
 - It has the tendency to spread the intensity values to span a larger range

Histogram Equalization Example



- Histograms have wider spread of intensity levels
- Notice the equalized images all have similar visual appearance
 - Even though histograms are different
 - Contrast enhancement

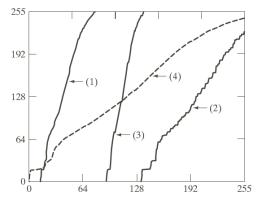


FIGURE 3.21
Transformation functions for histogram equalization.
Transformations (1) through (4) were obtained from the histograms of the images (from top to bottom) in the left column of Fig. 3.20 using Eq. (3.3-8).

Local Histogram Enhancement

- Global methods (like histogram equalization as presented) may not always make sense
 - What happens when properties of image regions are different?
- Compute histogram over smaller windows
 - Break image into "blocks"
 - Process each block separately

Original image



Block histogram equalization



 Notice the blocking effects that cause noticeable boundary effects

Local Enhancement

• Compute histogram over a block (neighborhood) for every pixel in a moving window

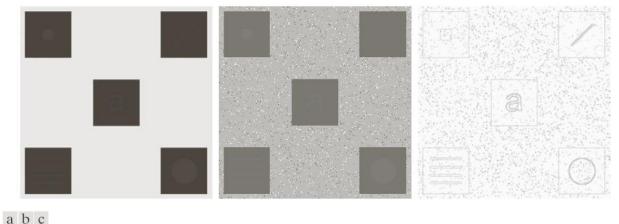


FIGURE 3.26 (a) Original image. (b) Result of global histogram equalization. (c) Result of local histogram equalization applied to (a), using a neighborhood of size 3×3 .

 Adaptive histogram equalization (AHE) is a computationally efficient method to combine block based computations through interpolation







Figure 3.8 Locally adaptive histogram equalization: (a) original image; (b) block histogram equalization; (c) full locally adaptive equalization.

Image Processing Motivation

- Image processing is useful for the reduction of noise
- Common types of noise
 - Salt and pepper random occurrences of black and white pixels
 - Impulse random occurrences of white pixels
 - Gaussian variations in intensity drawn from normal distribution



Original



Impulse noise



Salt and pepper noise



Gaussian noise

Ideal Noise Reduction

 How can we reduce noise given a single camera and a still scene?

Take lots of images and average them



What about if you only have a single image?

Image Filtering

- Filtering is a neighborhood operation
 - Use the pixels values in the vicinity of a given pixel to determine its final output value
- Motivation: noise reduction
 - Replace a pixel by the average value in a neighborhood
 - Assumptions:
 - Expect pixels to be similar to their neighbors (local consistency)
 - Expect noise processes to be independent from pixel to pixel (i.i.d.)

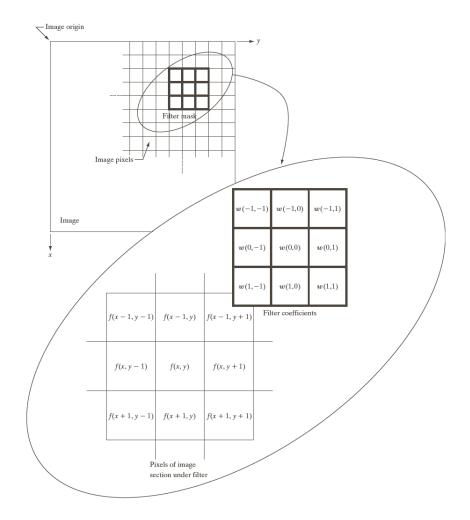
Linear Filtering

- Most common type of neighborhood operator
- Output pixel is determined as a weighted sum of input pixel values
 - $g(x,y) = \sum_{k,l} f(x+k,y+l)w(k,l)$
 - *w* is known as the kernel, mask, filter, template, or window
 - w(k, l) entry is known as a kernel weight or filter coefficient
- This is also known as the correlation operator

$$g = f \otimes w$$

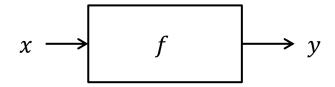
Filtering Operation

- $g(x,y) = \sum_{k,l} f(x+k,y+l)w(k,l)$
- The filter mask is moved from point to point in an image
 - The response is computed based on the sum of products of the mask coefficients and image
- Notice the mask is centered at w(0,0)
 - Usually we use odd sized masks so that the computation is symmetrically defined
- Matlab commands
 - imfilter.m, filter2.m, conv2.m

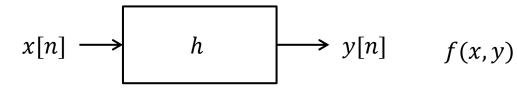


Connection to Signal Processing

General system notation



- LTI system
 - Convolution relationship
- Discrete 1D LTI system



$$y[n] = \sum_{k=-\infty}^{\infty} x[k]h[n-k]$$

Discrete 2D LTI system

$$f(x,y) \longrightarrow w \longrightarrow g(x,y)$$

$$g(x,y) = \sum_{s=-\infty}^{\infty} \sum_{t=-\infty}^{\infty} f(x,y)w(x-s,y-t)$$

 Linear filtering is the same as convolution without flipping

Border Effects

- The filtering process suffers from boundary effects
 - What should happen at the edge of an image?
 - No values exist outside of image
- Padding extends image values outside of the image to "fill" the kernel at the borders
 - Zero set pixels to o value
 - Will cause a darkening of the edges of the image
 - Constant set border pixels to fixed value
 - Clamp repeat edge pixel value
 - Mirror reflect pixels across image edge

Computational Requirements

- Convolution requires K^2 operations per pixel for a $K \times K$ size filter
- Total operations on an image is $M \times N \times K^2$
- This can be computationally expensive for large *K*
- Cost can be greatly improved if the kernel is separable
 - First do 1D horizontal convolution
 - Follow with 2D vertical convolution

- Separable kernel
 - $w = vh^T$
 - v vertical kernel
 - *h* horizontal kernel
 - Defined by outer product
- Can approximate a separable kernel using singular value decomposition (SVD)
 - Truly separable kernels will only have one non-zero singular value

Smoothing Filters

- Smoothing filters are used for blurring and noise reduction
 - Blurring is useful for small detail removal (object detection), bridging small gaps in lines, etc.
- These filters are known as lowpass filters
 - Higher frequencies are attenuated
 - What happens to edges?

Linear Smoothing Filter

- The simplest smoothing filter is the moving average or box filter
 - Computes the average over a constant neighborhood

$\frac{1}{\sqrt{2}}$	1	1		1
	1	1		1
	• • • •	• • • •	1	• • • •
	1	1	• • •	1

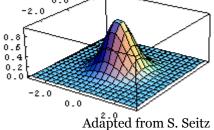
- This is a separable filter
 - Horizontal 1D filter

- $\frac{1}{K}$ 1 1 \cdots 1
- Remember your square wave from DSP
 - $h[n] = \begin{cases} 1 & 0 \le n \le M \\ 0 & \text{else} \end{cases}$
 - Fourier transform is a sinc function

More Linear Smoothing Filters

- More interesting filters can be readily obtained
- Weighted average kernel (bilinear) places more emphasis on closer pixels
 - More local consistency
- Gaussian kernel an approximation of a Gaussian function
 - Has variance parameter to control the kernel "width"
 - fspecial.m

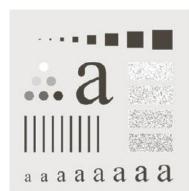
$$h(u,v) = \frac{1}{2\pi\sigma^2}e^{-\frac{u^2+v^2}{\sigma^2}}$$



c d

e f

Smoothing Examples



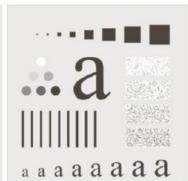


FIGURE 3.33 (a) Original image, of size 500×500 pixels. (b)–(f) Results of smoothing with square averaging filter masks of sizes m=3,5,9,15, and 35, respectively. The black squares at the top are of sizes 3,5,9,15,25,35,45, and 55 pixels, respectively; their borders are 25 pixels apart. The letters at the bottom range in size from 10 to 24 points, in increments of 2 points; the large letter at the top is 60 points. The vertical bars are 5 pixels wide and 100 pixels high; their separation is 20 pixels. The diameter of the circles is 25 pixels, and their borders are 15 pixels apart; their intensity levels range from 0% to 100% black in increments of 20%. The background of the image is 10% black. The noisy rectangles are of size 50×120 pixels.

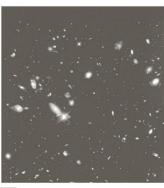


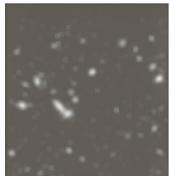






Object detection





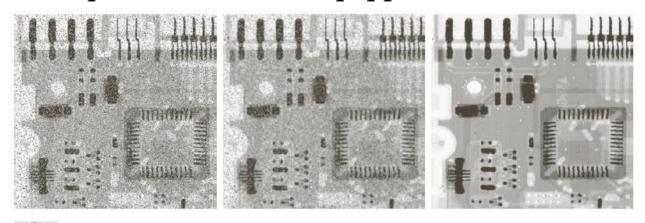


a b c

FIGURE 3.34 (a) Image of size 528×485 pixels from the Hubble Space Telescope. (b) Image filtered with a 15×15 averaging mask. (c) Result of thresholding (b). (Original image courtesy of NASA.)

Median Filtering

- Sometimes linear filtering is not sufficient
 - Non-linear neighborhood operations are required
- Median filter replaces the center pixel in a mask by the median of its neighbors
 - Non-linear operation, computationally more expensive
 - Provides excellent noise-reduction with less blurring than smoothing filters of similar size (edge preserving)
 - For impulse and salt-and-pepper noise



a b c

FIGURE 3.35 (a) X-ray image of circuit board corrupted by salt-and-pepper noise. (b) Noise reduction with a 3 × 3 averaging mask. (c) Noise reduction with a 3 × 3 median filter. (Original image courtesy of Mr. Joseph E. Pascente, Lixi, Inc.)

Bilateral Filtering

- Combine the idea of a weighted filter kernel with a better version of outlier rejection
 - α -trimmed mean calculates average in neighborhood excluding the α fraction that are smallest or largest
- $w(i,j,k,l) = d(i,j,k,l) \times r(i,j,k,l)$
 - d(i, j, k, l) domain kernel specifies "distance" similarity between pixels (usually Gauassian)
 - r(i, j, k, l) range kernel specifies "appearance (intensity)" similarity between pixels

Bilateral Filtering Example

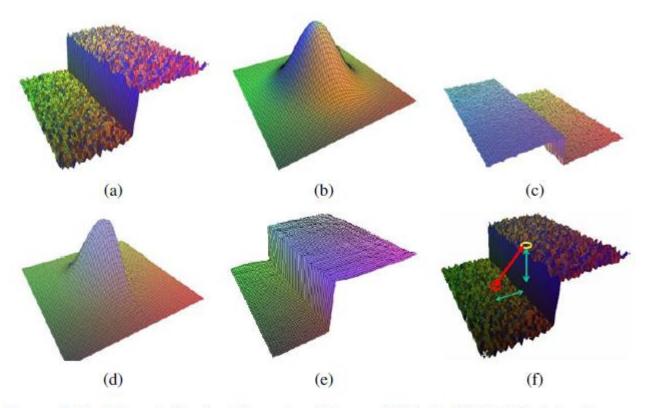


Figure 3.20 Bilateral filtering (Durand and Dorsey 2002) © 2002 ACM: (a) noisy step edge input; (b) domain filter (Gaussian); (c) range filter (similarity to center pixel value); (d) bilateral filter; (e) filtered step edge output; (f) 3D distance between pixels.

Sharpening Filters

- Sharpening filters are used to highlight fine detail or enhance blurred detail
- Smoothing we saw was averaging
 - This is analogous to integration
- Since sharpening is the dual operation to smoothing, it can be accomplished through differentiation

Digital Derivatives

- Derivatives of digital functions are defined in terms of differences
 - Various computational approaches
- Discrete approximation of a derivative

$$\frac{\partial f}{\partial x} = f(x+1) - f(x)$$

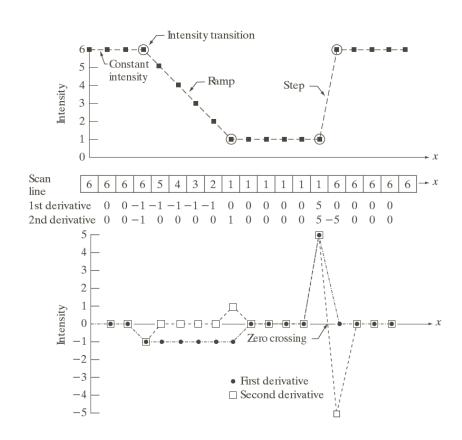
$$\frac{\partial f}{\partial x} = f(x+1) - f(x-1)$$

- Center symmetric
- Second-order derivative

$$\frac{\partial^2 f}{\partial x^2} = f(x+1) + f(x-1) - 2f(x)$$

Difference Properties

- 1st derivative
 - Zero in constant segments
 - Non-zero at intensity transition
 - Non-zero along ramps
- 2nd derivative
 - Zero in constant areas
 - Non-zero at intensity transition
 - Zero along ramps
- 2nd order filter is more aggressive at enhancing sharp edges
 - Outputs different at ramps
 - 1st order produces thick edges
 - 2nd order produces thin edges
 - Notice: the step gets both a negative and positive response in a double line



The Laplacian

- 2nd derivatives are generally better for image enhancement because of sensitivity to fine detail
- The Laplacian is simplest isotropic derivative operator

- Isotropic rotation invariant
- Discrete implementation using the 2nd derivative previously defined

$$\cdot \frac{\partial^2 f}{\partial x^2} = f(x+1,y) + f(x-1,y) - 2f(x,y)$$

•
$$\frac{\partial^2 f}{\partial x^2} = f(x, y+1) + f(x, y-1) - 2f(x, y)$$

Discrete Laplacian

- Zeros in corners give isotropic results for rotations of 90°
- Non-zeros corners give isotropic results for rotations of 45°
 - Include diagonal derivatives in Laplacian definition
- Center pixel sign indicates light-to-dark or dark-to-light transitions

0	1	0	1	1	1
1	-4	1	1	-8	1
0	1	0	1	1	1
0	-1	0	-1	-1	-1
-1	4	-1	-1	8	-1
0	-1	0	-1	-1	-1

a b c d

FIGURE 3.37

(a) Filter mask used to implement Eq. (3.6-6).

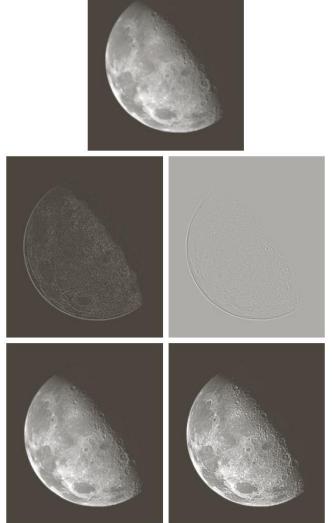
(b) Mask used to implement an extension of this equation that includes the diagonal terms.

(c) and (d) Two other implementations of the Laplacian found frequently in

practice.

Sharpening Images

- Sharpened image created by addition of Laplacian
 - $g(x,y) = \begin{cases} f(x,y) \nabla^2 f(x,y) & w(0,0) < 0 \\ f(x,y) + \nabla^2 f(x,y) & w(0,0) > 0 \end{cases}$
- Notice: the use of diagonal entries creates much sharper output image
- How can we compute g(x, y) in one filter pass without the image addition?
 - Think of a linear system

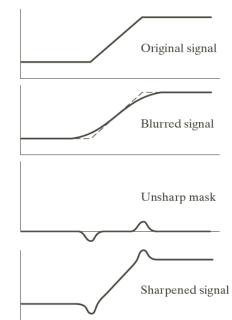


a b c d e

FIGURE 3.38 (a) Blurred image of the North Pole of the moon. (b) Laplacian without scaling. (c) Laplacian with scaling. (d) Image sharpened using the mask in Fig. 3.37(a). (e) Result of using the mask in Fig. 3.37(b). (Original image courtesy of NASA.)

Unsharp Masking

- Edges can be obtained by subtracting a blurred version of an image
 - $f_{us}(x,y) = f(x,y) \overline{f}(x,y)$
 - Blurred image
 - $\bar{f}(x,y) = h_{\text{blur}} * f(x,y)$
- Sharpened image
 - $f_s(x,y) = f(x,y) + \gamma f_{us}(x,y)$



a b c

FIGURE 3.39 1-D illustration of the mechanics of unsharp masking. (a) Original signal. (b) Blurred signal with original shown dashed for reference. (c) Unsharp mask. (d) Sharpened signal, obtained by adding (c) to (a).









DIP-XE



FIGURE 3.40

- (a) Original image.
- (b) Result of blurring with a Gaussian filter.
- (c) Unsharp mask. (d) Result of using unsharp masking.
- (e) Result of using highboost filtering.

The Gradient

- 1st derivatives can be useful for enhancement of edges
 - Useful preprocessing before edge extraction and interest point detection
- The gradient is a vector indicating edge direction

$$\nabla \mathbf{f} = \begin{bmatrix} G_x \\ G_y \end{bmatrix} = \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \end{bmatrix}$$

- The gradient magnitude can be approximated as

 - This give isotropic results for rotations of 90°

- Sobel operators
 - Have directional sensitivity
 - Coefficients sum to zero
 - Zero response in constant intensity region

-1	-2	-1	-1	0	1
0	0	0	-2	0	2
1	2	1	-1	0	1

 $G_{\mathcal{Y}}$ $G_{\mathcal{X}}$

Morphological Image Processing

- Filtering done on binary images
 - Images with two values [0,1], [0, 255], [black,white]
 - Typically, this image will be obtained by thresholding

•
$$g(x,y) = \begin{cases} 1 & f(x,y) > T \\ 0 & f(x,y) \le T \end{cases}$$

- Morphology is concerned with the structure and shape
- In morphology, a binary image is convolved with a structuring element *s* and results in a binary image
- See Chapter 9 of Gonzalez and Woods for a more complete treatment

Mathematical Morphology

- Tool for extracting image components that are useful in the representation and description of region shape
 - Boundaries, skeletons, convex hull, etc.
- The language of mathematical morphology is set theory
 - A set represents an object in an image
- This is often useful in video processing because of the simplicity of processing and emphasis on "objects"
 - Handy tool for "clean up" of a thresholded image

Morphological Operations

- Threshold operation
 - $\theta(f,t) = \begin{cases} 1 & f \ge t \\ 0 & \text{else} \end{cases}$
- Structuring element
 - $s e.g. 3 \times 3$ box filter (1's indicate included pixels in the mask)
 - S number of "on" pixels in s
- Count of 1s in a structuring element
 - $c = f \otimes s$
 - Correlation (filter) raster scan procedure

 Basic morphological operations can be extended to grayscale images

- Dilation
 - dilate $(f,s) = \theta(c,1)$
 - Grows (thickens) 1 locations
- Erosion
 - erode $(f,s) = \theta(c,S)$
 - Shrink (thins) 1 locations
- Opening
 - open(f,s) = dilate(erode(f,s),s)
 - Generally smooth the contour of an object, breaks narrow isthmuses, and eliminates thin protrusions
- Closing
 - $\operatorname{close}(f,s) = \operatorname{erode}(\operatorname{dilate}(f,s),s)$
 - Generally smooth the contour of an object, fuses narrow breaks/separations, eliminates small holes, and fills gaps in a contour

Morphology Example

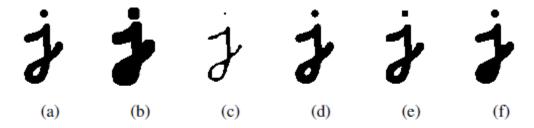


Figure 3.21 Binary image morphology: (a) original image; (b) dilation; (c) erosion; (d) majority; (e) opening; (f) closing. The structuring element for all examples is a 5×5 square. The effects of majority are a subtle rounding of sharp corners. Opening fails to eliminate the dot, since it is not wide enough.

- Dilation grows (thickens) 1 locations
- Erosion shrink (thins) 1 locations
- Opening generally smooth the contour of an object, breaks narrow isthmuses, and eliminates thin protrusions
- Closing generally smooth the contour of an object, fuses narrow breaks/separations, eliminates small holes, and fills gaps in a contour

Connected Components

- Semi-global image operation to provide consistent labels to similar regions
 - Based on adjacency concept
- Most efficient algorithms compute in two passes

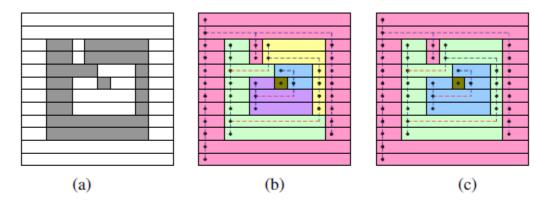


Figure 3.23 Connected component computation: (a) original grayscale image; (b) horizontal runs (nodes) connected by vertical (graph) edges (dashed blue)—runs are pseudocolored with unique colors inherited from parent nodes; (c) re-coloring after merging adjacent segments.

More computational formulations (iterative) exist from morphology

$$X_k = (X_{k-1} \oplus B) \cap A$$
 Set

More Connected Components

- Typically, only the "white" pixels will be considered objects
 - Dark pixels are background and do not get counted
- After labeling connected components, statistics from each region can be computed
 - Statistics describe the region e.g. area, centroid, perimeter, etc.

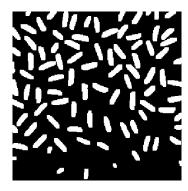
Matlab functions

- bwconncomp.m, labelmatrix.m (bwlabel.m)labelimage
- label2rgb.m color components for viewing
- regionprops.m calculate region statistics

Connected Component Example



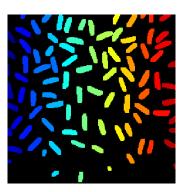
Grayscale image



Opened Image



Threshold image



Labeled image – 91 grains of rice